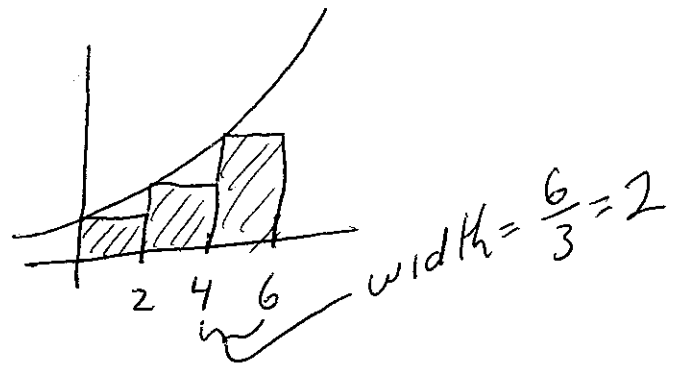


1.) Approximate $\int_0^6 e^x dx$ using

(a) 3 inscribed rectangles of equal width.

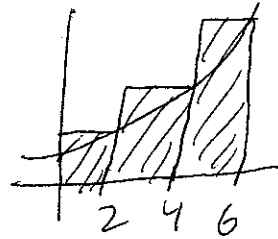
$$e^0(2) + e^2(2) + e^4(2)$$

$$= \boxed{2 + 2e^2 + 2e^4}$$



(b) 3 circumscribed rectangles of equal width.

$$\boxed{2e^2 + 2e^4 + 2e^6}$$

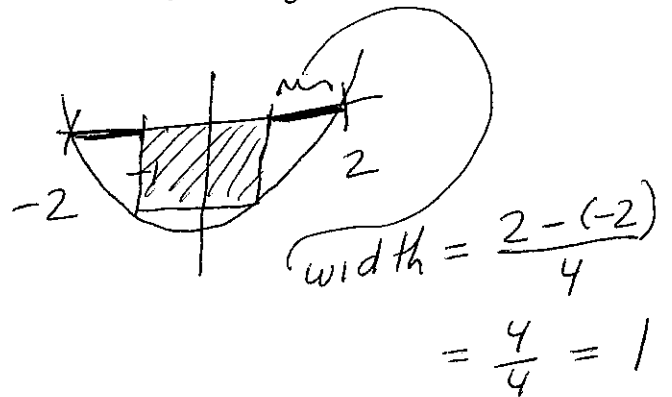


2.) Approximate $\int_{-2}^2 (x^2 - 4) dx$ using

(a) 4 inscribed rectangles of equal width.

$$(0)(1) + (-3)(1) + (-3)(1) + (0)(1)$$

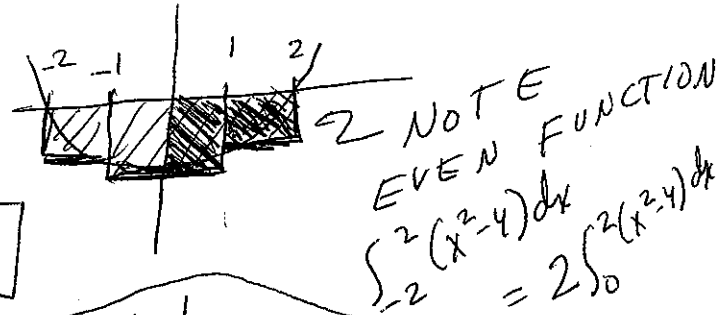
$$= 2(-3) = \boxed{-6}$$



(b) 4 circumscribed rectangles of equal width.

~~$$2(2) + 2(4)$$~~

$$2[(-4)(1) + (-3)(1)] = \boxed{-14}$$

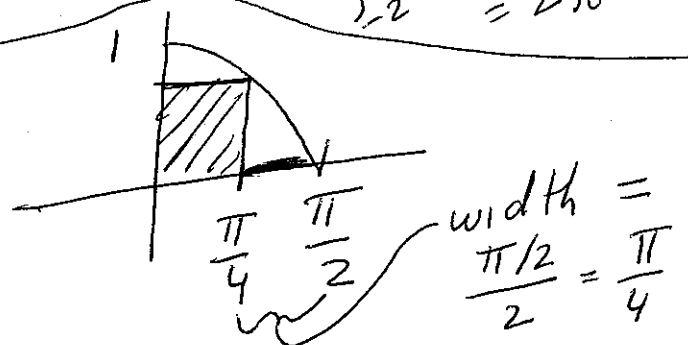


3.) Approximate $\int_0^{\pi/2} \cos(x) dx$ using

(a) 2 inscribed rectangles of equal width.

$$\cos\left(\frac{\pi}{4}\right) \cdot \frac{\pi}{4} + 0 \cdot \frac{\pi}{4}$$

$$= \frac{\sqrt{2}}{2} \cdot \frac{\pi}{4} = \boxed{\frac{\pi\sqrt{2}}{8}}$$



(b) 2 circumscribed rectangles of equal width.

$$\cos(0) \cdot \frac{\pi}{4} + \cos\left(\frac{\pi}{4}\right) \cdot \frac{\pi}{4}$$

$$= \frac{\pi}{4} + \frac{\sqrt{2}}{2} \cdot \frac{\pi}{4} = \boxed{\frac{(2 + \sqrt{2})\pi}{8}}$$

