## 22M174/22C174: Optimization techniques.

## Homework 1. Due 02/04/13.

- 1. Prove Theorem I.2.1.1.
- 2. Prove Lemma I.2.2.9.
- 3. Find the stationary points of the three following objective functions

$$\begin{aligned} f_1(x_1, x_2) &= 2\cos(x_1)x_2 + x_2^2, \\ f_2(x_1, x_2) &= 3x_1^2 + 2x_2^4 - 8x_2^2 - 10, \\ f_3(x_1, x_2) &= 12x_1x_2(x_1 - x_2 + 1) + 4x_2^3 - 6x_2^2. \end{aligned}$$

Which of these points are local minimizers, local maximizers, or saddle points?

- 4. Is  $[0,0,0]^T$  a local minimizer of  $f(x_1, x_2, x_3) = 4x_1^2 + 2x_3 \cos(3x_2)$ ? If not, find points arbitrarily close to  $[0,0,0]^T$  with a lower function value.
- 5. Show that  $[0,0]^T$  is a local minimizer of  $f(x_1, x_2) = (x_1 2x_2^2)(x_1 8x_2^2)$ along every line passing through  $[0,0]^T$ . Show also that  $f(3x_2^2, x_2) < f(0,0)$  if  $x_2 \neq 0$ .