

The final will cover from Chapter 12 to 15.

There will be an extra review at 4:10pm Sunday December 15.

1. Find the tangent plane of $xu(x, y) + y(u(x, y))^2 = 2x^2$ at the point $(1, 1, 1)$.
Find the tangent plane of $x^2 + y^2 + 2z^2 = 4$ at $(1, 1, 1)$.
2. Plot level curves for the function
 $z = f(x, y) = 4x^2 + y^2$.
Plot the level surfaces of the function $f(x, y, z) = x^2 + y^2 + 4z^2$.
3. Find the direction in which the function $z = 2x + \sin(2y - x)$ increases the most from the point $(0, 0)$.
4. Find the directional derivative of $z = f(x, y) = 4x^2 + y^2$ in the direction of $i + j$ at the point $(1, 1)$.
What is physical meaning of this derivative?
5. Compute: $(x^y)_{x, y}$.
6. Find tangent, normal vector and curvature of the curve:
 $ti + tj + t^2 k$.
7. A particle's acceleration is according to
 $a(t) = \sin t i - t j + t^2 k$. Find all its possible vector-valued position function.
8. Find parametrizations of the curves $4x^2 + y^2 = 1$ and $\frac{1}{4}x^2 + y^2 = 1$.
9. Find maxima and maximal value of the function $2x - y$ inside the unit circle.
10. Find the integral $\int \int \int_D x^2 d\text{vol}$, where D is the upper half unit ball
 $x^2 + y^2 + z^2 \leq 1, z \geq 0$.
11. Find maxima and maximal value of the function $x^2 + 2y$ in the triangle
 $x + 3y = 1, y = 0$ and $x = 0$.
12. Find the integral $\int \int \int_D x d\text{vol}$, where D is the part of the unit ball
 $x^2 + y^2 + z^2 \leq 1$ and $x \geq 0, y \geq 0, z \geq 0$.
13. Find the extrema of the function x^2y in the triangle bounded by the
 x -axis
and y -axis and the line $x + y = 1$.
14. Compute $\int \int_D x^2 y dx dy$, where D is the upper half disk.
15. Compute the divergence and curl of the vector fields $x^2y i + \cos(x + y)j + zk$. The physical meaning of divergence is the density of the source of the vector field and that for curl is the vector valued circulation density.
16. Compute $\int_C yx dx + xdy$, where C is the counterclockwise unit circle.
17. Compute $\int_S x^2 ds$, where S is the upper half circle.
18. Compute the center of mass of unit circle with density $d(x, y) = x^2$.
19. Write down the change of variable formulae for

spherical and cylindrical coordinates.

20. Compute the integral

$$\int \int_{x^2+4y^2 \leq 4} (x+y^2) dx dy.$$

21. Compute $\int \int_{\Sigma} F \cdot n dS$ where Σ is the region bounded by the upper half sphere

$$\text{and } F = xy^2i + (x+y)j + zk.$$

22. Compute $\int_C F \cdot dr$, where $F = x^2yi + (x+y)j + zk$ and C is the intersection of the unit sphere and the plane $x = z$, with the right hand orientation.

23. Compute $\int \int_{\Sigma} F dS$ where Σ is the region bounded by the upper half sphere

$$\text{and } F = z.$$

24. Approximate $\sqrt{99}$ and $\sin(46^\circ)$. You have to show the formula. An answer

from calculate will yield 0 point.

25. Find the maximum of xyz if $x + y + z = 1$ and positive.